

OPEN Real world ocean rogue waves explained without the modulational instability

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Since the 1990s, the modulational instability has commonly been used to explain the occurrence of roque waves that appear from nowhere in the open ocean. However, the importance of this instability in the context of ocean waves is not well established. This mechanism has been successfully studied in laboratory experiments and in mathematical studies, but there is no consensus on what actually takes place in the ocean. In this work, we question the oceanic relevance of this paradigm. In particular, we analyze several sets of field data in various European locations with various tools, and find that the main generation mechanism for roque waves is the constructive interference of elementary waves enhanced by second-order bound nonlinearities and not the modulational instability. This implies that roque waves are likely to be rare occurrences of weakly nonlinear random seas.

According to the most commonly used definition, rogue waves are unusually large-amplitude waves that appear from nowhere in the open ocean. Evidence that such extremes can occur in nature is provided, among others, by the Draupner and Andrea events, which have been extensively studied over the last decade¹⁻⁶. Several physical mechanisms have been proposed to explain the occurrence of such waves⁷, including the two competing hypotheses of nonlinear focusing due to third-order quasi-resonant wave-wave interactions⁸, and purely dispersive focusing of second-order non-resonant or bound harmonic waves, which do not satisfy the linear dispersion relation^{9,10}.

In particular, recent studies propose third-order quasi-resonant interactions and associated modulational instabilities^{11,12} inherent to the Nonlinear Schrödinger (NLS) equation as mechanisms for rogue wave formation^{3,8,13-15}. Such nonlinear effects cause the statistics of weakly nonlinear gravity waves to significantly differ from the Gaussian structure of linear seas, especially in long-crested or unidirectional (1D) seas^{8,10,16-19}. The late-stage evolution of modulation instability leads to breathers that can cause large waves^{13–15}, especially in 1D waves. Indeed, in this case energy is 'trapped' as in a long wave-guide. For small wave steepness and negligible dissipation, quasi-resonant interactions are effective in reshaping the wave spectrum, inducing large breathers via non-linear focusing before wave breaking occurs^{16,17,20,21}. Consequently, breathers can be observed experimentally in 1D wave fields only at sufficiently small values of wave steepness^{20–22}. However, wave breaking is inevitable when the steepness becomes larger: 'breathers do not breathe'²³ and their amplification is smaller than that predicted by the NLS equation, in accord with theoretical studies²⁴ of the compact Zakharov equation^{25,26} and numerical studies of the Euler equations^{27,28}.

Typical oceanic wind seas are short-crested, or multidirectional wave fields. Hence, we expect that nonlinear focusing due to modulational effects is diminished since energy can spread directionally 16,18,29 . Thus, modulation instabilities may play an insignificant role in the wave growth especially in finite water depth where they are further attenuated30

Tayfun³¹ presented an analysis of oceanic measurements from the North Sea. His results indicate that large waves (measured as a function of time at a given point) result from the constructive interference (focusing) of elementary waves with random amplitudes and phases enhanced by second-order non-resonant or bound nonlinearities. Further, the surface statistics follow the Tayfun³² distribution³² in agreement with observations^{9,10,31,33}. This is confirmed by a recent data quality control and statistical analysis of single-point measurements from fixed sensors mounted on offshore platforms, the majority of which were recorded in the North Sea³⁴. The analysis of

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	Andrea	Draupner	Killard
Significant wave height H _s [m]	10.0	11.2	11.4
Dominant wave period T_p [s]	14.3	15.0	17.2
Mean zero-crossing wave period T_0 [s]	11.6	12.1	14.0
Mean wavelength L_0 [m]	209	219	268
Depth d [m], k_0d	74, 2.23	70, 2.01	58, 1.36
Spectral bandwidth ν	0.35	0.36	0.37
Angular spreading σ_{θ}	0.37	0.39	0.34
Parameter $R = \sigma_{\theta}^2/2\nu^{240}$	0.56	0.59	0.42
Benjamin Feir Index BFI in deep water ⁸	0.24	0.23	0.18
Depth factor α_S^{40}	0.31	0.36	0.04
Tayfun NB skewness $\lambda_{3,NB}^{-41}$	0.159	0.165	0.145
Mean skewness λ_3 from HOS simulations	0.141	0.146	0.142
Maximum NB dynamic excess kurtosis $\lambda^d_{40, \mathrm{max}}$ 29	$2.3 \cdot 10^{-3}$	$2.1 \cdot 10^{-3}$	$2.7 \cdot 10^{-4}$
Janssen NB bound excess kurtosis $\lambda_{40,NB}^{\ b}{}^{45}$	0.065	0.074	0.076
Mean excess kurtosis λ_{40} from HOS simulations	0.041	0.032	-0.011
Janssen NB setdown ST_{NB}/H_s^{45} , predicted HOS setdown	0.12, 0.08	0.1, 0.11	0.1, 0.07
Maximum crest height h/H _s : observed, numerical	1.63, 1.71	1.55, 1.54	1.44, 1.57
Maximum crest-to-trough (wave) height H/H _s : observed, numerical	2.30, 2.51	2.10, 2.23	2.00, 2.28
Maximum trough-to-crest (wave) height H/H,: observed, numerical	2.49, 2.67	2.15, 2.09	2.32, 2.29

Table 1. Wave parameters and various statistics of the simulated sea states labelled Andrea, Draupner and Killard. The Killard rogue wave occurred on a water depth of 39 m, however the hincast input spectrum could only be computed at an averaged water depth of 58 m. Statistical parameters are from an ensemble of 50 HOS simulations of sea states. We refer to the Methods section for the definitions of the wave parameters. Note that two wave heights are given for each wave: the zero-downcrossing value (crest to trough) and the zero-upcrossing value (trough to crest).

an ensemble of 122 million individual waves revealed 3649 rogue events, concluding that rogue waves observed at a point in time are merely rare events induced by dispersive focusing. Thus, a wave whose crest height exceeds the rogue threshold 2 1.25 H_s occurs on average once every $N_r \sim 10^4$ waves with N_r referred to as the return period of a rogue wave and H_s is the significant wave height. Some even more recent measurements off the west coast of Ireland 35 revealed similar statistics with 13 rogue events out of an ensemble of 750873 individual waves and $N_r \sim 6 \cdot 10^4$.

To date, it is still under debate if in typical oceanic seas second-order nonlinearities dominate the dynamics of extreme waves as indicated by ocean measurements^{31,33}, or if third-order nonlinear effects play also a significant, if not dominant, role in rogue-wave formation. The preceding provides our principal motivation for studying the statistical and physical properties of rogue sea states and to investigate the relative importance of second and third-order nonlinearities. We rely on WAVEWATCH III hindcasts and High Order Spectral (HOS) simulations of the Euler equations for water waves³⁶. In our study, we consider the famous Draupner and Andrea rogue waves and the less well known Killard rogue wave³⁵. The Andrea rogue wave was measured by Conoco on 9 November 2007 with a system of four Teledyne Optech lasers mounted in a square array on the Ekofisk platform in the North Sea in a water depth $d = 74 \,\mathrm{m}^{4.5}$. The metocean conditions of the Andrea wave are similar to those of the Draupner wave measured by Statoil at a nearby platform ($d = 70 \,\mathrm{m}$) on 1 January 1995 with a down looking laser-based wave sensor³⁷. The Killard wave was measured by ESB International on 28 January 2014 by a Waverider buoy off the west coast of Ireland in a water depth d = 39 m. In Table 1 we summarize the wave parameters of the three sea states in which the rogue wave occurred and we refer to the Methods section for definitions and details. As one can see, the actual crest-to-trough (wave) heights H and crest heights h meet the classical criteria $^2H/H_s>2$ and $h/H_s > 1.25$ to qualify the Andrea, Draupner and Killard extreme events as rogue waves. The remainder of the paper is organized as follows. First, the probability structure of oceanic seas is presented³³ together with the essential elements of Tayfun's³² second-order theory for the wave skewness and Janssen's⁸ formulation for the excess kurtosis of multidirectional seas²⁹. Then, we present and compare second-order and third-order statistical properties of the three rogue sea states followed by an analysis of the shape of the largest waves and associated mean sea levels. In concluding, we discuss the implications of these results on rogue-wave predictions.

Probability structure of oceanic seas

Non-resonant and resonant wave-wave interactions cause the statistics of weakly nonlinear gravity waves to significantly differ from the Gaussian structure of linear seas^{8,10,16–18,38}. The relative importance of ocean nonlinearities and the increased occurrence of large waves can be measured by integral statistics such as the wave skewness λ_3 and the excess kurtosis λ_{40} of the zero-mean surface elevation $\eta(t)$:

$$\lambda_3 = \overline{\eta^3}/\sigma^3, \qquad \lambda_{40} = \overline{\eta^4}/\sigma^4 - 3.$$
 (1)

Here, overbars imply statistical averages and σ is the standard deviation of surface wave elevations. Here and in the following we refer to the Methods section for the definitions of the wave parameters and details.

The skewness coefficient represents the principal parameter with which we describe the effects of second-order bound nonlinearities on the geometry and statistics of the sea surface with higher sharper crests and shallower more rounded troughs 9,32,33 . The excess kurtosis comprises a dynamic component due to third-order quasi-resonant wave-wave interactions and a bound contribution induced by both second- and third-order bound nonlinearities 9,10,32,33,39,40 . In order to compare the relative orders of nonlinearities, we consider the characteristic wave steepness $\mu_m = k_m \sigma$, where k_m is the wavenumber corresponding to the mean spectral frequency ω_m^{32} .

Return period of a wave whose crest height exceeds a given threshold

To describe the statistics of rogue waves, we consider the conditional return period $N_h(\xi)$ of a wave whose crest height exceeds the threshold $h = \xi H_o$ namely

$$N_h(\xi) = \frac{1}{\Pr[h > \xi H_s]} = \frac{1}{P(\xi)},$$
 (2)

where $P(\xi)$ is the probability of a wave crest height exceeding ξH_s . Equation (2) implies that the threshold ξH_s , with $H_s = 4\sigma$, is exceeded on average once every $N_h(\xi)$ waves.

For weakly nonlinear random seas, the probability P can be described by the (third-order) TF, (second-order Tayfun) T or (linear Rayleigh) R distributions. In particular³³,

$$P_{TF}(\xi) = \Pr[h > \xi H_s] = \exp(-8\xi_0^2)[1 + \Lambda \xi_0^2 (4\xi_0^2 - 1)], \tag{3}$$

where ξ_0 follows from the quadratic equation $\xi = \xi_0 + 2\mu \xi_0^{232}$. Here, the wave steepness $\mu = \lambda_3/3$ is of $O(\mu_m)$ and it is a measure of second-order bound nonlinearities as it relates to the skewness of surface elevations⁹. The relationship $\lambda_3 = 3\mu$ is originally due to Tayfun³¹, who derived it for narrowband nonlinear waves that display a vertically asymmetric profile with sharper and higher crests and shallower and more rounded troughs. As such this sort of asymmetry is also reflected in a quantitative sense in the skewness coefficient λ_3 of surface elevations from the mean sea level. Although the relationship was thought to be appropriate to only narrowband waves, Fedele & Tayfun⁹ have more recently verified that it is also valid for broadband waves. In simple terms, $\mu = \lambda_3/3$ serves as a convenient relative measure of the characteristic crest-trough asymmetry of ocean waves. For narrowband (NB) waves in intermediate water depth, Tayfun⁴¹ derived a compact expression that reduces to the simple form $\lambda_{3,NB} = 3\mu_m$ in deep water³² (see Methods section for details). The parameter Λ in Eq. (3) is a measure of third-order nonlinearities as a function of the fourth order cumulants of the wave surface³³. Our studies show that it is approximated by $\Lambda_{appr} = 8\lambda_{40}/3$ (see Methods section). For second-order seas, hereafter referred to as Tayfun sea states⁴², $\Lambda = 0$ only and P_{TF} in Eq. (3) yields the Tayfun (T) distribution³²

$$P_T(\xi) = \exp(-8\xi_0^2) = \exp\left[-\frac{(-1 + \sqrt{1 + 8\mu\xi})^2}{2\mu^2}\right]. \tag{4}$$

For Gaussian seas, $\mu = 0$ and $\Lambda = 0$ and P_{TF} reduces to the Rayleigh (R) distribution

$$P_R(\xi) = \exp(-8\xi^2).$$
 (5)

We point out that the Tayfun distribution represents an exact result for large second order wave crest heights and it depends solely on the steepness parameter defined as $\mu = \lambda_3/3^9$. In the following, we will not dwell on wave heights ^{43,44} as our main focus will be the statistics of crest heights in oceanic rogue sea states.

Excess kurtosis

For third-order nonlinear random seas the excess kurtosis

$$\lambda_{40} = \lambda_{40}^d + \lambda_{40}^b \tag{6}$$

For deep-water narrowband waves characterized by a Gaussian type directional spectrum, the six-fold integral can be reduced to a one-fold integral, so that the dynamic excess kurtosis is computed as²⁹

$$\lambda_{40}^{d} = 6BFI^{2} \text{ Im } \int_{0}^{\nu^{2}\omega_{m}t} \frac{1}{\sqrt{1 - 2i\alpha + 3\alpha^{2}}\sqrt{1 + 2iR\alpha + 3R^{2}\alpha^{2}}} d\alpha,$$
 (7)

where ω_m is the mean spectral frequency, ν the spectral bandwidth, $i=\sqrt{-1}$ and $\mathrm{Im}(x)$ denotes the imaginary part of x. In the focusing regime (0 < R < 1) the dynamic excess kurtosis of an initially homogeneous Gaussian wave field grows, attaining a maximum at the intrinsic time scale $\tau_c = \nu^2 \omega_m t_c = 1/\sqrt{3R}$. Thus, the sea state initially deviates from being Gaussian, but eventually the excess dynamic kurtosis tends monotonically to zero as energy spreads directionally, in agreement with numerical simulations⁴⁸. The dynamic excess kurtosis maximum is well approximated by²⁹

$$\lambda_{40, \text{ max}}^d \approx 3BFI^2 \frac{b}{(2\pi)^2} \frac{1-R}{R+bR_0}, \qquad 0 \le R \le 1,$$
 (8)

where $R_0 = 3\sqrt{3}/4\pi^3$ (which corrects a misprint in²⁹) and b = 2.48. In contrast, in the defocusing regime (R > 1) the dynamic excess kurtosis is always negative. It reaches a minimum at t_c and then tends to zero over larger periods of time. In summary, the theoretical predictions indicate a decaying trend for the dynamic excess kurtosis over large times in multidirectional wave fields (R > 0).

In unidirectional (R=0) seas, energy is 'trapped' as in a long wave-guide. An initially homogeneous Gaussian wave field evolves as the dynamic excess kurtosis monotonically increases toward an asymptotic non-zero value given by $\lambda_{40,NLS}^d = 3BFI^2\pi/(3\sqrt{3})$ from Eq. (8)⁴⁹. Clearly, wave energy cannot spread directionally, and quasi-resonant interactions induce nonlinear focusing and large breather-type waves initiated by modulation instability ^{16,17,20-23,50}. However, realistic oceanic wind seas are typically multidirectional (short-crested) and energy can spread directionally. As a result, nonlinear focusing due to modulational instability effects diminishes ^{16,18,29,51} or becomes essentially insignificant under realistic oceanic conditions ²⁹. Indeed, the large excess kurtosis transient observed during the initial stage of evolution is a result of the unrealistic assumption that the initial wave field is homogeneous Gaussian whereas oceanic wave fields are usually statistically inhomogeneous both in space and time. Further, for time scales $t \gg t_c$, starting with initial homogeneous and Gaussian conditions becomes irrelevant as the wave field tends to a non-Gaussian state dominated by bound nonlinearities as the total kurtosis of surface elevations asymptotically approaches the value represented by the bound component ^{52,53}.

These results and conclusions hold for deep-water gravity waves. The extension to intermediate water depth d readily follows by redefining the Benjamin-Feir Index as $BFI_S^2 = \alpha_S BFI^2$ 40.54, where the depth factor α_S depends on the dimensionless depth $k_m d$, with k_m the wavenumber corresponding to the mean spectral frequency (see Methods section). In the deep-water limit α_S becomes 1. As the dimensionless depth $k_m d$ decreases, α_S decreases and becomes negative for $k_m d < 1.363$ and so does the dynamic excess kurtosis. For the three rogue sea states under study, depth factors are less than 1 and given in Table 1 together with the associated BFI and R coefficients. From Eq. (8), the maximum dynamic excess kurtosis is of $O(10^{-3})$ for all three sea states and thus negligible in comparison to the associated narrowband (NB) bound component $\lambda_{40,NB}^b$ of $O(10^{-2})$ (see Methods section). Hereafter, this will be confirmed further by a quantitative analysis of High Order Spectral (HOS) simulations of the Euler equations 36 .

Results

At present, whether second-order or third-order nonlinearities play a dominant role in rogue-wave formation is a subject of considerable debate. Recent theoretical results clearly show that third-order quasi-resonant interactions play an insignificant role in the formation of large waves in realistic oceanic seas²⁹. Further, oceanic evidence available so far^{31,33,34} seems to suggest that the statistics of large oceanic wind waves are not affected in any discernible way by third-order nonlinearities, including NLS-type modulational instabilities that attenuate as the wave spectrum broadens²⁴. Indeed, extensive analyses of storm-generated extreme waves do not display any data trend even remotely similar to the systematic breather-type patterns observed in 1D wave flumes^{10,31,33,34}. However, third-order bound nonlinearities may affect both skewness and kurtosis as they shape the wave surface with sharper crests and shallower troughs.

In the following we will compare second and third-order nonlinear properties of the sea states where the Draupner, Andrea and Killard rogue waves occurred, using HOS simulations of the Euler equations³⁶. To do so, we first use WAVEWATCH III to hindcast the three rogue sea states. The respective directional spectra $\mathbf{S}(\omega,\theta)$ are shown in Fig. 1. These are used to define the initial wave field conditions for the HOS simulations–see the Methods section.

Second-order vs third-order nonlinearities. The time evolutions of skewness and excess kurtosis of the three simulated rogue sea states are shown in Fig. 2. Initially, the two statistics undergo a brief artificial transient of O(10) mean wave periods during which nonlinearities are smoothly activated by way of a ramping function⁵⁵ applied to the HOS equations. Following this stage, we do not observe the typical overshoot beyond the Gaussian value as seen in wave tank measurements and simulations^{8,16,17,50}. In contrast, both statistics rapidly reach a steady state as an indication that quasi-resonant wave-wave interactions due to modulation instabilities are negligible in agreement with theoretical predictions²⁹. Indeed, the large-time kurtosis is mostly Gaussian for all the three sea states and there are insignificant differences between second-order and third-order HOS simulations. Further, Fig. 2 shows that the narrowband predictions slightly overestimate the observed simulated values for skewness and excess kurtosis. This is simply because narrowband approximations do not take into account the directionality and the finite bandwidth of the spectrum.

Our main conclusion is that second-order bound nonlinearities mainly affect the large-time skewness λ_3 whereas excess kurtosis is smaller since it is of $O(\lambda_3^2)^{39,40}$ (see also Methods section). Clearly, second-order effects are the dominant factors in shaping the probability structure of the random sea state with a minor contribution of

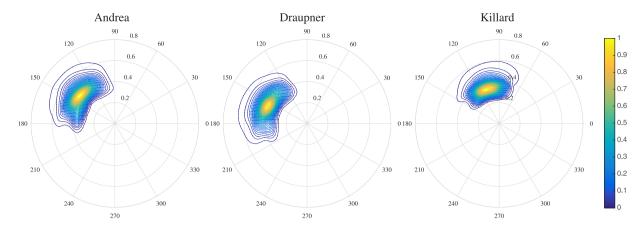


Figure 1. WAVEWATCH III hindcast directional wave spectra $S(\omega, \theta)$ used as input for the HOS simulations. Here, ω is the angular frequency and θ the direction in degrees. (Left) Andrea, (center) Draupner, (right) Killard. The spectra have been normalized with respect to spectral peak values.

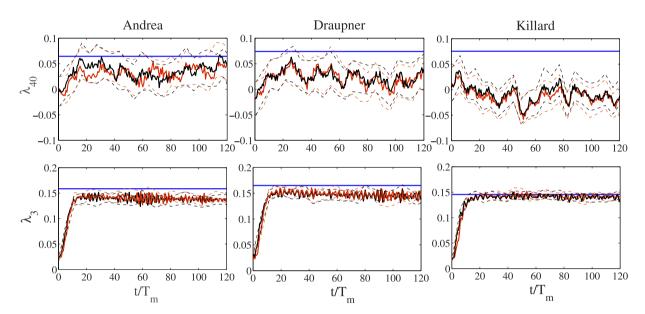


Figure 2. Time evolution of skewness λ_3 and excess kurtosis λ_{40} for (left) Andrea, (center) Draupner and (right) Killard sea states; HOS second-order (black solid), HOS third-order (red solid) averages and theoretical predictions of the narrowband Tayfun skewness and Janssen excess bound kurtosis (blue solid, see Eq. (9) in Methods Section). 95% confidence bands (dashed) are also shown. Time is normalized by the mean wave period T_m . The statistical parameters are estimated from an ensemble of 50 HOS simulations. The initial artificial transients are excluded from the ensemble averages as they are the result of a ramping function 55 applied to the HOS equations to smoothly activate nonlinearities. See Methods section for details and definitions of wave parameters.

excess kurtosis effects. Such dominance is seen in Fig. 3, where the HOS numerical predictions of the conditional return period $N_h(\xi)$ of a crest exceeding the threshold ξH_s are compared against the theoretical predictions based on the linear Rayleigh (R), second-order Tayfun (T) and third-order (TF) models from Eq. (3). In particular, $N_h(\xi)$ follows from Eq. (2) as the inverse $1/P(\xi)$ of the empirical probabilities of a crest height exceeding the threshold ξH_s . An excellent agreement is observed between simulations and the third-order TF model, which is nearly the same as the second-order T model. This indicates that second-order effects are dominant, whereas the linear Rayleigh model underestimates the empirical return periods.

For both second- and third-order nonlinearities, the return period N_r of a wave whose crest height exceeds the rogue threshold $1.25H_s$ is nearly $2 \cdot 10^4$ for the Andrea, Draupner and Killard sea states. Oceanic rogue wave measurements³⁴ indicate that the rogue threshold for crest heights is exceeded on average once every $N_r \sim 10^4$ waves. Similarly, recent measurements off the west coast of Ireland³⁵ yield $N_r \sim 6 \cdot 10^4$. In contrast, in a Gaussian sea the same threshold is exceeded more rarely and on average once every $3 \cdot 10^5$ waves.

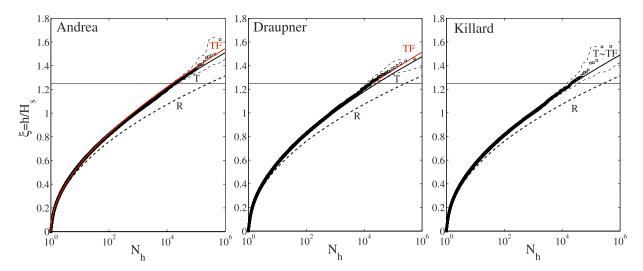


Figure 3. Crest height scaled by the significant wave height (ξ) versus conditional return period (N_h) for the (left) Andrea, (center) Draupner and (right) Killard rogue sea states: HOS numerical predictions (\Box) in comparison with theoretical models (T = second-order Tayfun (light solid lines), TF = third-order (red solid lines) and R = Rayleigh distributions (dark dashes)). Confidence bands are also shown (light dashes). $N_h(\xi)$ is the inverse of the exceedance probability $P(\xi) = Pr[h > \xi H_s]$. Horizontal lines denote the rogue threshold $1.25H_s^2$.

Note that all three rogue waves have crest heights that exceed the threshold $1.5H_s$. This is exceeded on average once every $5 \cdot 10^5$ waves in second- and third-order seas and extremely rarely in Gaussian seas, i.e. on average once every $6 \cdot 10^7$ waves. This implies that the three rogue wave crest events are likely to be rare occurrences of weakly second-order random seas, or Tayfun sea states⁴². Our results clearly confirm that rogue wave generation is the result of the constructive interference (focusing) of elementary waves enhanced by second-order nonlinearities in agreement with the theory of stochastic wave groups proposed by Fedele and Tayfun⁹, which relies on Boccotti's⁴³ theory of quasi-determinism⁴³. Our conclusions are also in agreement with observations^{9,10,31,33}.

Comparison of the profiles of three rogue waves. For all three rogue sea states under study, the largest wave observed in the HOS simulations is now compared against the actual rogue wave measurements. Figure 4 compares the actual wave profiles (thin solid line) with the largest second-order (thin dotted-dashed line) and third-order (thick solid line) simulated waves. While there are small differences between the two orders, second-order nonlinearities are sufficient in predicting the observed profiles with sufficient accuracy.

In the same figure, the simulated mean sea level (MSL) below the crests is also shown. The estimation of the MSL follows by low-pass filtering the measured time series of the wave surface with frequency cutoff $f_c \sim f_p/2$, where f_p is the frequency of the spectral peak⁵⁶. Note that the time series must be long enough and contain at least ~200 waves for a statistically robust estimation of wave-wave interactions. In shorter time series, a set-up is observed as a manifestation of the large crest segment that extends above the adjacent lower crests. The HOS simulations give approximately the same MSL for both second- and third-order nonlinearities predicting a setdown below the large crests as expected from theory⁵⁷. However, the observed Draupner set-up (thin line) is not reproduced by our HOS numerical simulations (see Fig. 4). We also note that the HOS MSL is close to the narrowband prediction ST_{NB} (see Table 1 and Methods section for definitions). The actual MSL for Andrea is not available, and buoy observations give neither a set-up nor a set-down for Killard.

Taylor *et al.*⁵⁸ reported that for the Draupner wave the hindcast from the European Centre for Medium-Range Weather Forecasts shows swell waves propagating at approximately 80 degrees to the wind sea. They argued that the Draupner wave may be due to the crossing of two almost orthogonal wave groups in accord with second-order theory. This would explain the set-up observed under the large wave⁵⁶ instead of the second-order set-down normally expected⁵⁷. Note that the angle between the two dominant sea directions lies outside the range ~20–60 degrees where modulation instability is enhanced⁵⁹.

Further studies and a high resolution hindcast of the Draupner sea state are needed to clarify if it was a crossing-seas situation as our WAVEWATCH III hindcast spectrum does not indicate so. Concerning the disagreement for the Draupner wave on the set-up, we have conducted numerical HOS experiments where the input spectrum consists of two identical JONSWAP type crossing sea states at 90 degrees. And we indeed found a set-up. As a matter of fact, whether one obtains a set-up or a set-down depends on the angle between the crossing seas. As the angle increases, the set-down turns into a set-up – see Fig. 5. However, we still find that second-order effects are dominant and third-order contributions on skewness and kurtosis, mainly due to bound nonlinearities, are negligible.

Our results are in agreement with the recent numerical simulations by Trulsen *et al.*⁴² of the crossing sea state encountered during the accident of the tanker Prestige on 13 November 2002. Puzzled by the literature on crossing seas states, they checked whether the fact that the accident occurred during a bimodal sea state with two wave

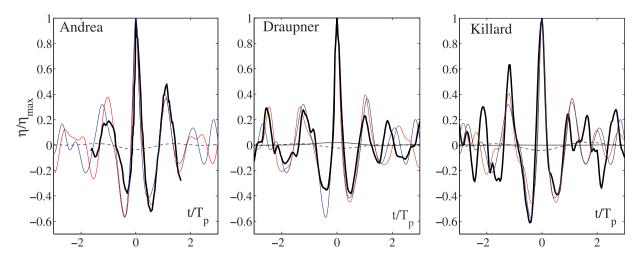


Figure 4. Third-order HOS simulated extreme wave profiles (red thin solid), second-order HOS profiles (blue thin solid) and mean sea levels (MSL) (thin dashed) versus the dimensionless time t/T_p for (left) Andrea, (center) Draupner and (right) Killard waves. For comparisons, measurements (thick solid) and actual MSLs (thin solid) are also shown. Note that the Killard MSL is insignificant and the Andrea MSL is not available. T_p is the dominant wave period (see Methods section for definitions).

systems crossing nearly at a right angle increased or not the chance of encountering a rogue wave. They concluded that the wave conditions at the time of the accident were only slightly more extreme than those of a Gaussian sea state, and slightly less extreme than those of a second-order Tayfun sea state³².

Discussion

Since the 1990s, modulational instability 11,12 of a class of solutions to the NLS equation has been proposed as a mechanism for rogue wave formation $^{3,8,13-15}$. The availability of exact analytical solutions of 1D NLS breathers 13 via the Inverse Scattering Transform 60 enormously stimulated new research on rogue waves. In particular, it has been found that in 1D wave fields, the late-stage evolution of modulation instability leads to large waves in the form of breathers $^{13-15}$. Indeed, in such situations energy is 'trapped' as in a long wave-guide, and quasi-resonant interactions are effective in inducing large breathers via nonlinear modulation before wave breaking occurs 16,17,20,21 . However, rogue waves in the form of breathers can be observed experimentally in 1D waves only at sufficiently small values of wave steepness ($\sim 0.01-0.09)^{20-22}$. Indeed, wave breaking is inevitable for wave steepness larger than 0.1: 'breathers do not breathe' 23 , and their amplification is smaller than that predicted by the NLS equation, as confirmed by numerical simulations 27,28 .

Clearly, typical oceanic wind seas are short-crested, or multidirectional wave fields and their dynamics is more 'free' than the 1D 'long-wave-guide' counterpart. Indeed, energy can spread directionally and as a result nonlinear focusing due to modulational instability is diminished ^{16,18,29}. Our results suggest that in typical oceanic fields third-order nonlinearities do not play a significant role in the wave growth.

Furthermore, we found that skewness effects on crest heights are dominant in comparison to bound kurtosis contributions and statistical predictions can be based on second-order models^{32,33,61}. Thus, rogue waves are likely to be rare occurrences resulting from the constructive interference (dispersive and directional focusing) of elementary waves enhanced by second order nonlinear effects in agreement with observations^{9,10,31,33} and with the theory of stochastic wave groups⁹. This theory about the mechanics of wave groups shows that they can be thought of as genes of a non-Gaussian sea dominated by second-order nonlinearities, when interested in the dynamics of large surface displacements. The space-time evolution of wave crests during an extreme event can be seen in the Supplementary Video S1 of the simulated Killard rogue wave sea state analyzed in this paper. We anticipate that our results may motivate similar analysis of waves over a wider distribution of heights using extensive data sets³⁴.

Methods

Wave parameters. The significant wave height H_s is defined as the mean value $H_{1/3}$ of the highest one-third of wave heights. It can be estimated either from a zero-crossing analysis or more easily from the wave omnidirectional spectrum $S(\omega) = \int_0^{2\pi} \mathbf{S}(\omega, \theta) d\theta$ as $H_s \approx 4\sigma$, where $\sigma = \sqrt{m_0}$ is the standard deviation of surface elevations, $m_i = \int S(\omega) \omega^i d\omega$ are spectral moments and $\mathbf{S}(\omega, \theta)$ is the directional wave spectrum.

The dominant wave period $T_p=2\pi/\omega_p$ refers to the frequency ω_p of the spectral peak. The mean zero-crossing wave period T_0 is equal to $2\pi/\omega_0$, with $\omega_0=\sqrt{m_2/m_0}$. The associated wavelength $L_0=2\pi/k_0$ follows from the linear dispersion relation $\omega_0=\sqrt{gk_0\tanh(k_0d)}$, with d the water depth. The mean spectral frequency is defined as $\omega_m=m_1/m_0^{32}$ and the associated mean period T_m is equal to $2\pi/\omega_m$. A characteristic wave steepness is defined as $\mu_m=k_m\sigma$, where k_m is the wavenumber corresponding to the mean spectral frequency ω_m^{32} . The following quantitites are also introduced: $q_m=k_md$, $Q_m=\tanh q_m$, the phase velocity $c_m=\omega_m/k_m$, the group velocity $c_g=c_m[1+2q_m/\sin(2q_m)]/2$. The spectral bandwidth $\nu=(m_0m_2/m_1^2-1)^{1/2}$ gives a measure of the frequency broadening. The

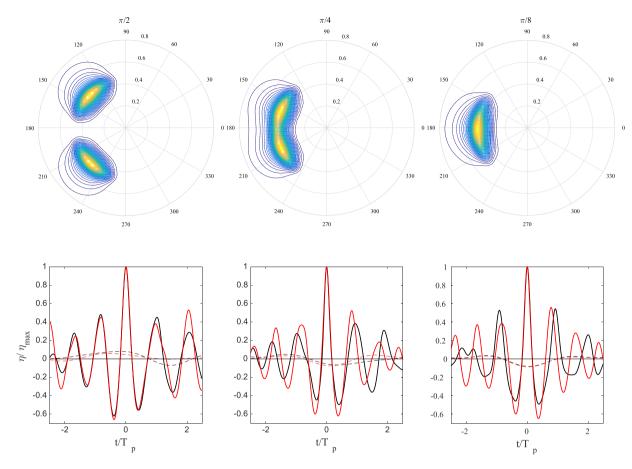


Figure 5. Upper row: crossing directional wave spectra $S(\omega,\theta)$ computed using two identical JONSWAP spectra with Draupner spectral properties. Lower row: extreme wave profiles simulated with third order HOS (red lines) and second order HOS (black lines). In addition, the corresponding mean sea levels are shown (dashed lines). The mean sea levels are scaled by three for emphasis. Crossing angles from left to right: $\pi/2$, $\pi/4$, and $\pi/8$. Note that for the final case, the relatively small crossing angle results in the spectrum appearing to contain only one dominant peak.

angular spreading is estimated as $\sigma_{\theta} = (2(1-\sqrt{a^2+b^2}/m_0))^{1/2}$, where $a=\int_0^{2\pi}\int_0^{\infty}\cos(\theta)\mathbf{S}(\omega,\,\theta)d\,\omega\,d\,\theta$ and $b=\int_0^{2\pi}\int_0^{\infty}\sin(\theta)\mathbf{S}(\omega,\,\theta)d\,\omega\,d\,\theta^{62}$. Note that $\omega_0=\omega_m\sqrt{1+\nu^2}$.

The parameter $\Lambda=\lambda_{40}+2\lambda_{22}+\lambda_{04}$ is a measure of third-order nonlinearities and is a function of the fourth order cumulants λ_{nm} of the wave surface η and its Hilbert transform $\hat{\eta}^{33}$. In particular, $\lambda_{22}=\overline{\eta^2\hat{\eta}^2}/\sigma^4-1$ and $\lambda_{04}=\overline{\hat{\eta}^4}/\sigma^4-3$. In practice, Λ is usually approximated solely in terms of the excess kurtosis as $\Lambda_{\rm appr}=8\lambda_{40}/3$ by assuming the relations between cumulants⁴⁹ $\lambda_{22}=\lambda_{40}/3$ and $\lambda_{04}=\lambda_{40}$. These, to date, have been proven to hold for linear and second-order narrowband waves only³⁹. For third-order nonlinear seas, our numerical studies indicate that $\Lambda\approx\Lambda_{\rm appr}$ within a 3% relative error in agreement with observations^{19,63}.

The wave steepness $\mu = \lambda_3/3$ relates to the wave skewness λ_3 of surface elevations. For narrowband (NB) waves in intermediate water the wave skewness⁴¹ and bound excess kurtosis⁴⁵

$$\lambda_{3,NB} = 6\mu_m(\alpha + \Delta), \quad \lambda_{40,NB}^b = 24\mu_m^2(\beta + \gamma + 2(\alpha + \Delta)^2) = \frac{4}{3}\lambda_{3,NB}^2 \left[1 + \frac{\beta + \gamma}{2(\alpha + \Delta)^2}\right],\tag{9}$$

where

$$\alpha = \frac{3 - Q_m^2}{4Q_m^3}, \quad \beta = \frac{24 + 3(1 - Q_m^2)^3}{64Q_m^6}, \quad \gamma = -\frac{\alpha^2}{2}, \quad \Delta = -\frac{1}{4}\frac{c_S^2}{c_S^2 - c_g^2} \left[2\frac{1 - Q_m^2}{Q_m} + \frac{1}{q_m} \right], \tag{10}$$

with $c_S = \sqrt{gd}$ the phase velocity in shallow water. The wave-induced set-down or mean sea level variation below a crest of amplitude h is $ST_{NB} = \Delta h^{245}$. In deep water,

$$\lambda_{3,NB} = 3\mu_m, \qquad \lambda_{40,NB}^b = 18\mu_m^2 = 2\lambda_{3,NB}^2.$$
 (11)

Note that Eq. (9) are not valid in small water depth as second and third-order terms of the associated Stokes expansion can be larger than the linear counterpart (see Eq. (A18) in⁴⁵). To be valid, the constraints $\alpha\mu_m \leq 1$ and $\beta\mu_m/\alpha \leq 1$ must hold. And indeed they are satisfied for the three rogue sea states under study. The depth factor α_s depends on $k_m d$ through of a lengthy expression, which is not reported here for the sake of simplicity – see Janssen and Onorato⁵⁴.

Brief description of WAVEWATCH III and hindcast validation. WAVEWATCH III^{62,64} is a third generation wave model developed at NOAA/NCEP that solves the spectral energy action balance equation with a source function representing the wind input, wave-wave interactions and the wave energy dissipation due to diverse processes. The configuration of the model was set to solve the balance equation from a minimum frequency of 0.0350 Hz up to 0.5552 Hz for 36 directional bands and 30 frequencies. A JONSWAP spectrum was set as an initial condition at every grid point. We used the wind input fields from the NOAA Climate Forecast System Reanalysis (CFSR)⁶⁴.

Higher Order Spectral Method. The HOS method is a numerical pseudo spectral method to solve the Euler equations governing the dynamics of incompressible fluid flow at a desired level of nonlinearity. In particular, the time evolution of the free surface of the fluid, $\eta(x, y, t)$, and the associated velocity potential $\psi(x, y, t)$ evaluated on the free surface are obtained. The method was independently developed in 1987 by Dommermuth & Yue³⁶ and West $et\ al.^{65}$. Within the present work, West $et\ al.^{6}$ s version is employed. Tanaka⁶⁶ provides a thorough description of the method.

Initial conditions for the potential ψ and surface elevation η are obtained from the directional spectrum as an output of WAVEWATCH III. In the wavenumber domain, the Fourier transform $\hat{\eta}(\mathbf{k})$ of η is constructed as $S(\mathbf{k})$ exp $(i\beta)$, where β is normally distributed over $[0,2\pi]$. Similarly, the Fourier transform $\hat{\psi}(\mathbf{k})$ of ψ is obtained via linear wave theory, and finally an inverse Fourier transform is applied. The numerical simulation is performed using 1024×1024 Fourier modes and over a time scale $T/T_m \sim O(\mu_m^{-2})$, where μ_m represents a characteristic wave steepness defined above. A low-pass filter is applied to avoid numerical blow-up.

Finally, we note that the use of the WAVEWATCH III model combined with HOS simulations may prove useful in assessing recently proposed techniques for rogue wave predictability based on chaotic time series analysis^{67,68} and third-order probabilistic models of unexpected wave extremes⁶⁹.

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Author Contributions

The concept and design was provided by F.F., who coordinated the scientific effort together with F.D. S.P.D.L. and J.B. performed numerical simulations and developed specific codes for the analysis. The wave statistical analysis was performed by F.F. together with J.B. The overall supervision was provided by F.F. and F.D. F.D. and J.D. made ongoing incisive intellectual contributions. All authors participated in the analysis and interpretation of results and the writing of the manuscript.

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